

**Graphing Parabolas By Completing the Square**

Complete the following table:

Trinomial $x^2 + bx + c$	Value of $b$	Value of $c$	Factored Form $(x-h)^2$	Value of $h$
$x^2 + 2x + 1$	2	1	$(x+1)^2$	-1
$x^2 + 8x + 16$	8	16	$(x+4)^2$	-4
$x^2 - 14x + 49$	-14	49	$(x-7)^2$	7
$x^2 - 6x + 9$	-6	9	$(x-3)^2$	3

Notice each of the trinomials in the first column is a perfect square trinomial which can be expressed in the form  $(x-h)^2$ .

In each row of the above table, what is the relation between  $b$  and  $c$ ?  $c$  is  $(\frac{1}{2}b)^2$

Between  $b$  and  $h$ ?  $h = \frac{b}{-2}$

\*\*\*\*\*

Previously, we graphed parabolas written in the form  $y = a(x-h)^2 + k$  (Vertex form).

But the equation of a parabola can also be written in the general quadratic form  $y = ax^2 + bx + c$  (standard form).

To graph a parabola written in this form, we must first complete the square.

Standard  
 Eg. 1 Graph  $y = x^2 + 6x + 7$  by first completing the square.

$y = x^2 + 6x + 9 - 9 + 7$  → take  $\frac{1}{2}$  of 6 square  
 Add/subtract that amount  
 $y = (x+3)^2 - 2$  → factor first 3 terms as perfect square  
 vertex form → vertex (-3, -2)

check: Expand + simplify to change vertex form → standard form.

$$\begin{aligned}
 y &= (x+3)^2 - 2 \\
 &= (x+3)(x+3) - 2 \\
 &= x^2 + 6x + 9 - 2 \rightarrow y = x^2 + 6x + 7
 \end{aligned}$$

Eg. 2 Graph  $y = 2x^2 - 8x + 5$  by first completing the square.

\* factor out coefficient of  $x^2$  term from first 2 terms

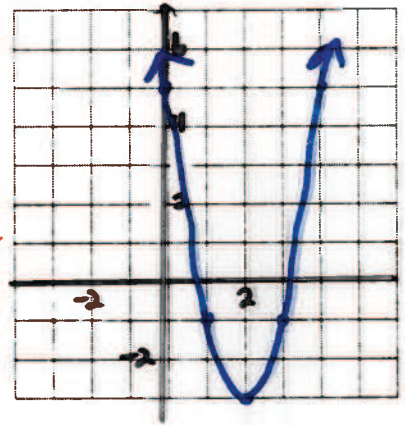
$$y = 2(x^2 - 4x) + 5$$

↑ take  $\frac{1}{2}$  + square it  
add / subtract that amount

$$y = 2(x^2 - 4x + 4 - 4) + 5$$

$$y = 2(x - 2)^2 - 8 + 5$$

$$y = 2(x - 2)^2 - 3 \quad \text{vertex } (2, -3)$$



Eg. 3 Graph  $y = 6x - 3x^2$  by first completing the square.

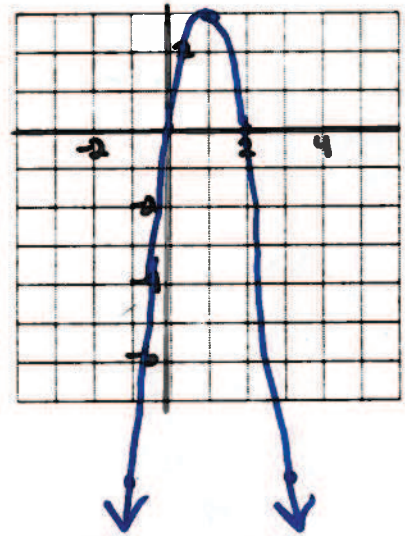
$$y = -3x^2 + 6x$$

$$y = -3(x^2 - 2x)$$

$$y = -3(x^2 - 2x + 1 - 1)$$

$$y = -3(x - 1)^2 + 3$$

vertex (1, 3)



Homework:

Pg 234 # 2 ac, 3, 4 ac, 5 ac, 6 ac, 8 ac